## ACCURATE ESTIMATION OF DIFFUSION COEFFICIENTS AND THEIR UNCERTAINTIES FROM COMPUTER SIMULATION

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THE OPTIMAL SCHEME TO ESTIMATE THE DIFFUSION COEFFICIENT REQUIRES BOTH VARIANCE AND COVARIANCE TO BE CONSIDERED.



## A COVARIANT MULTI-DIMENSIONAL NORMAL DISTRIBUTION CAN BE USED AS A GENERATIVE MODEL FOR MEAN-SQUARED DISPLACEMENT ...



DATA FROM MOLECULAR DYNAMICS SIMULATION CAN BE USED TO PARAMETERISE THE MODEL.



WE CAN SAMPLE THE PARAMETERISED DISTRIBUTION LIKELIHOOD WITH A HEAVISIDE PRIOR TO GET AN ESTIMATE OF THE DIFFUSION COEFFICIENT DISTRIBUTION, WHICH WOULD TYPICALLY REQUIRE MANY 10005 OF SIMULATIONS.

THIS IS A BAYESIAN SAMPLING APPROACH THAT USES MARKOV CHAIN MONTE CARLO ....



...AND USING THIS METHOD, ON 4096 INDIVIDUAL SIMULATIONS, GIVES AN UNBIASED, EFFICIENT ESTIMATE OF  $D^*$  WITH GOOD VARIANCE ESTIMATE.

